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# EXperiments Along Coexistence near Tricriticality

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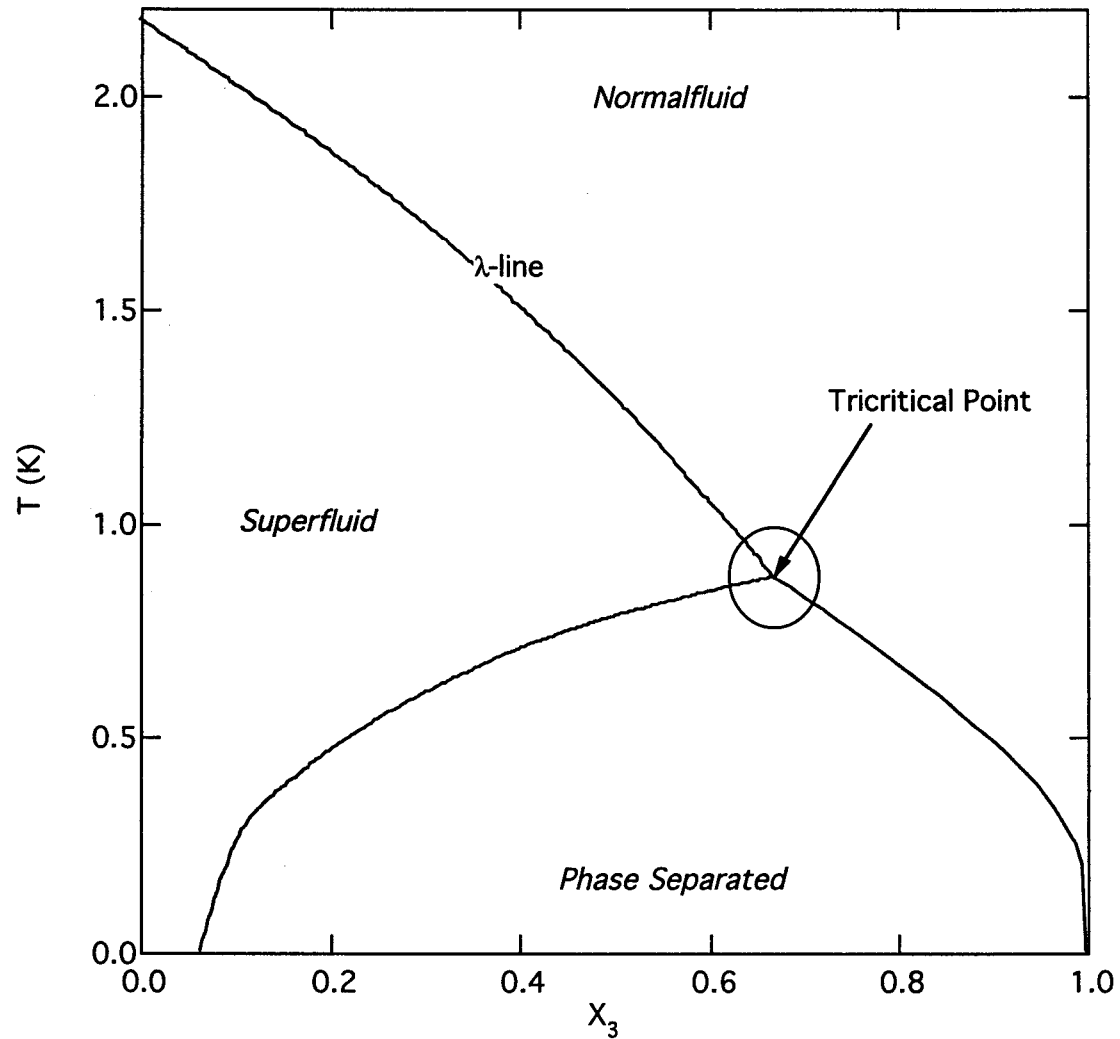
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# Helium Mixture Phase Diagram



# Why Study the Tricritical Point

- Tricritical points are model systems with 2 control parameters
- Theoretical predictions are exact for 3D tricritical points
  - predict integer fractions for the critical exponents
  - Predict logarithmic corrections to the power laws
- Existing experimental measurements not as accurate as at critical points
- Significant new technology available since previous work, 15-20 years ago
  - Higher resolution/stability thermometry
  - Improved second sound detectors

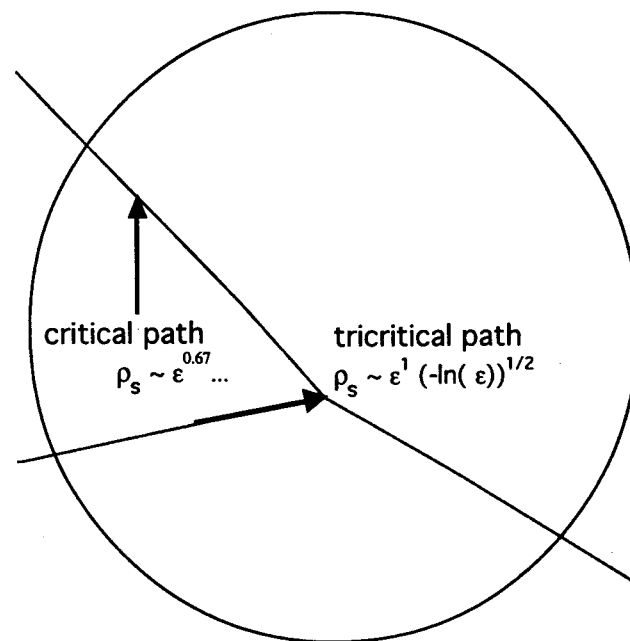
# Experimental Objectives

- Second sound measurements along the coexistence curve

$$\rho_s/\rho = \kappa_\sigma \varepsilon_t^{\zeta_\sigma} |\ln \varepsilon_t|^y$$

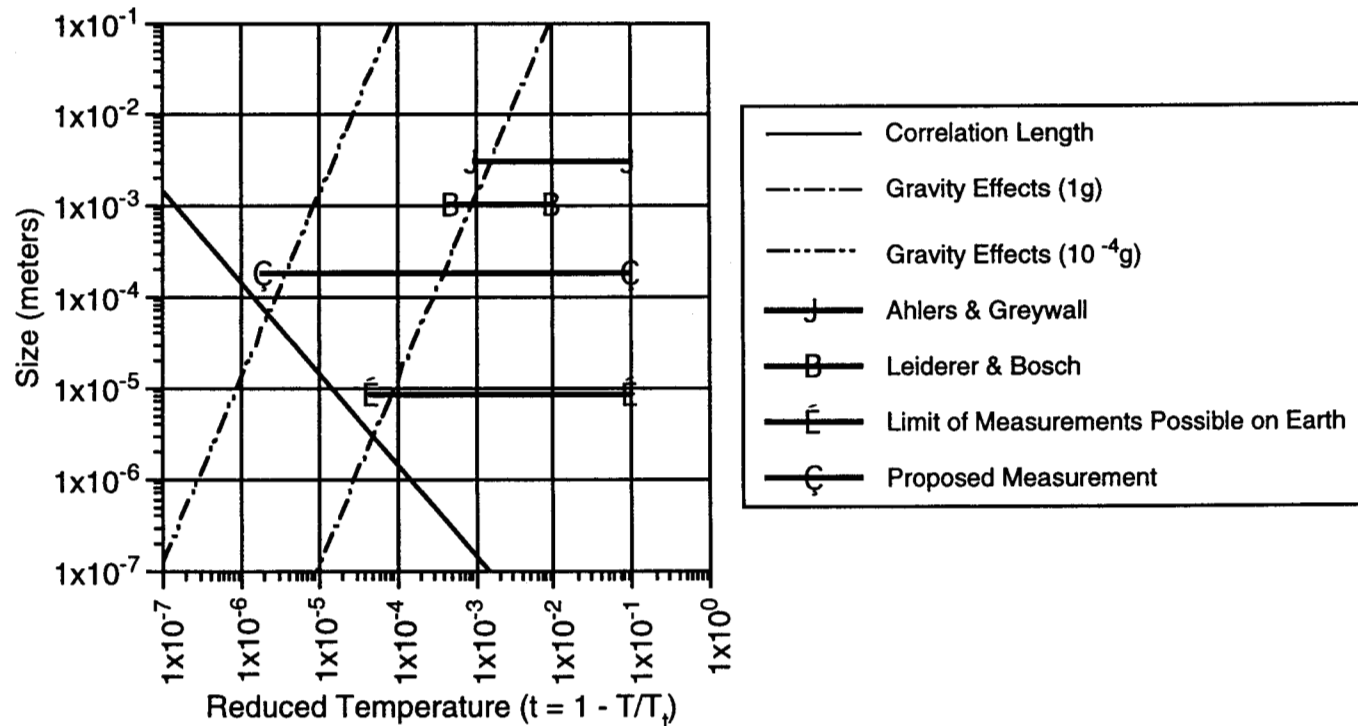
$$\zeta_\sigma = 1, y = 1$$

- Shape of the phase boundaries
  - power laws (exponents of 1)  
with logarithmic corrections

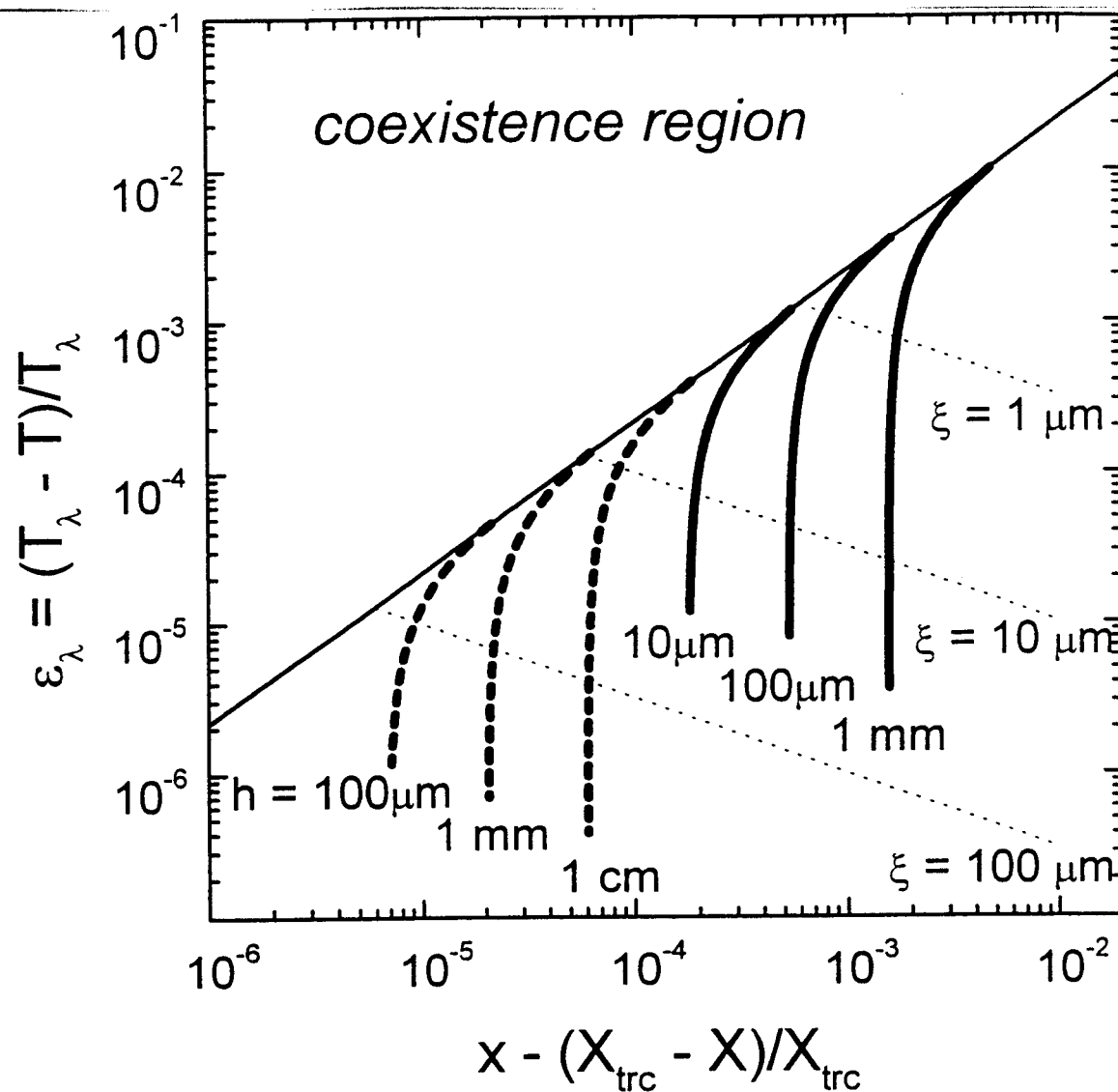


# Limitations Imposed by Gravity

- Concentration susceptibility diverges at tricritical point
  - small cell
- $\xi_0(X)$  diverges at tricritical point
  - large cell



# Gravity Effects: Concentration versus reduced T



## Other Complications

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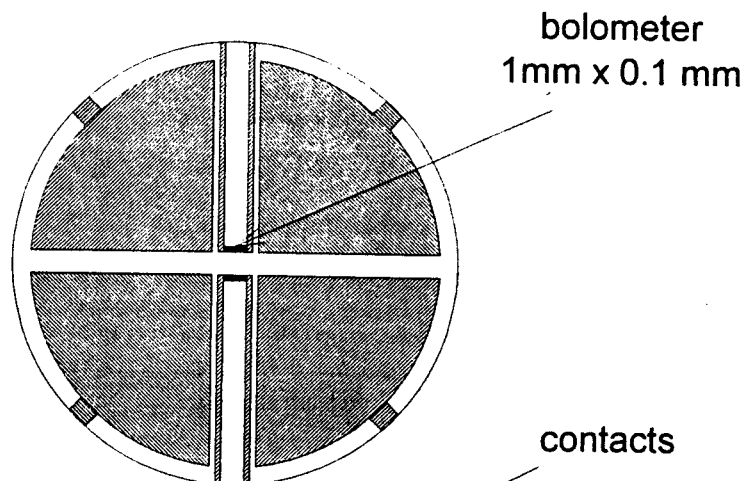
- The superfluid density is very small
  - Large counter flow velocities
  - Small second sound signals
  - Finite size effects become strong
- Long relaxation times
- Combined with gravity effects, sets experimental procedure
  - Thin flat cell
  - Pulsed time of flight second sound measurements



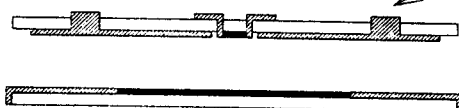
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# Experimental Cell

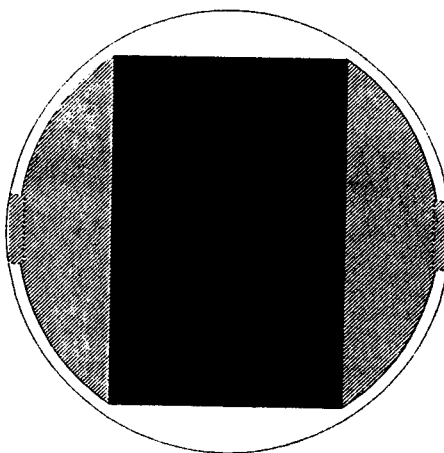
Bolometer side  
inside view



Top and bottom  
spaced 150mm apart



Heater side  
inside view

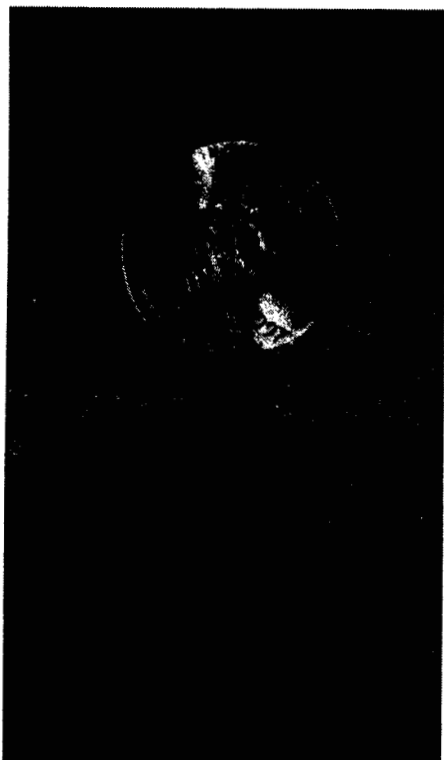


3/4"

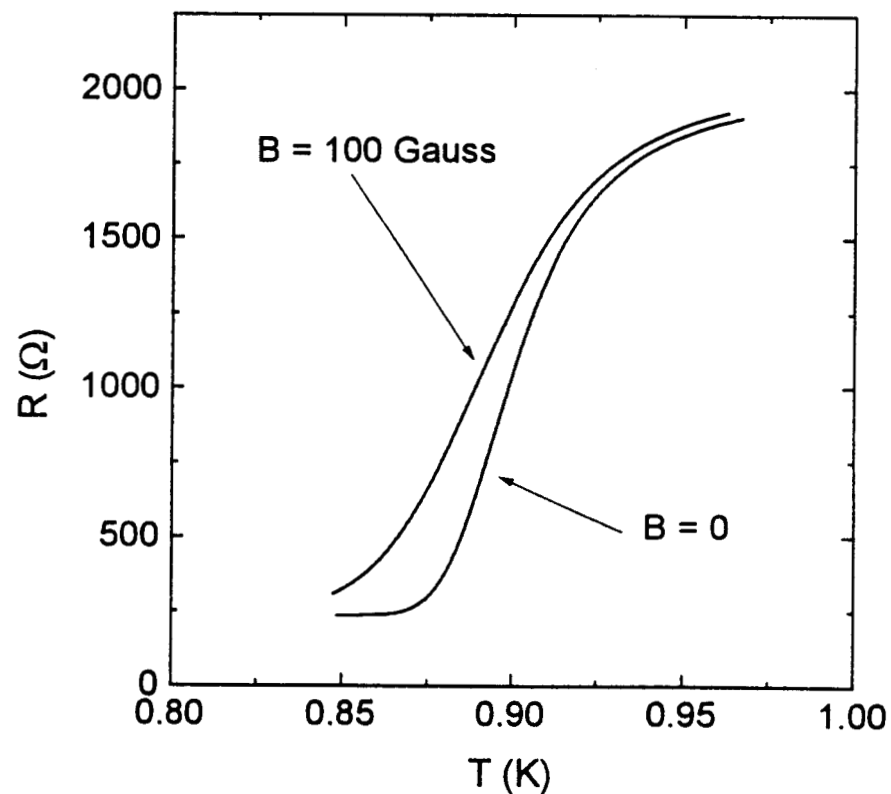


## Second Sound Detection

- Superconducting transition edge bolometers
  - Very thin films of tantalum
    - Reproducible properties
    - Transition can be shifted by magnetic field
    - High sensitivity



**Tantalum superconducting edge bolometer**



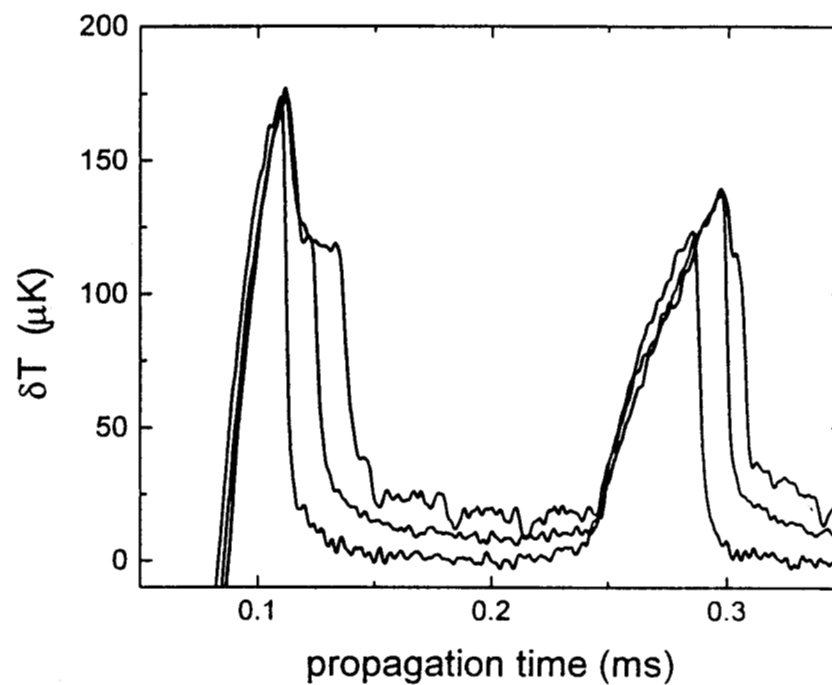
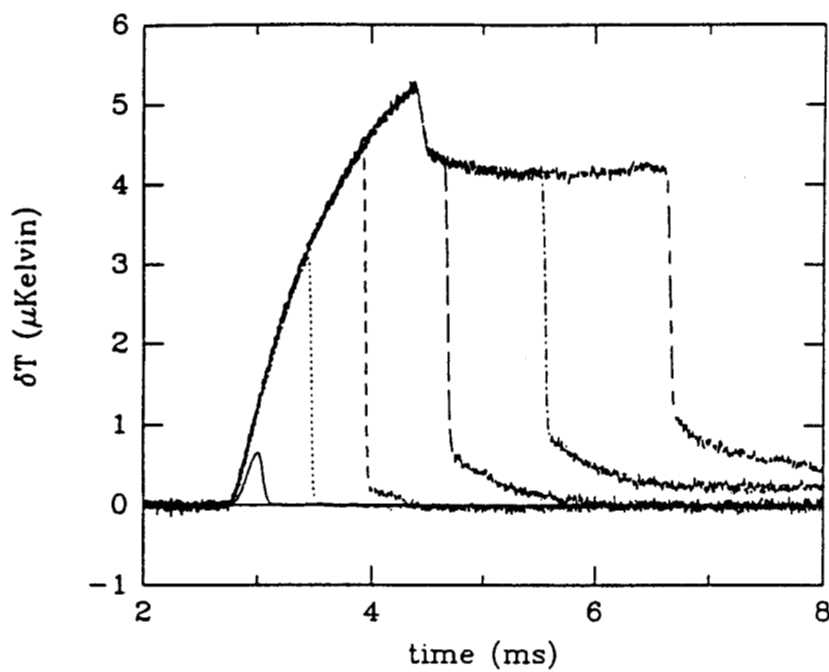
# Non-Linear Second Sound

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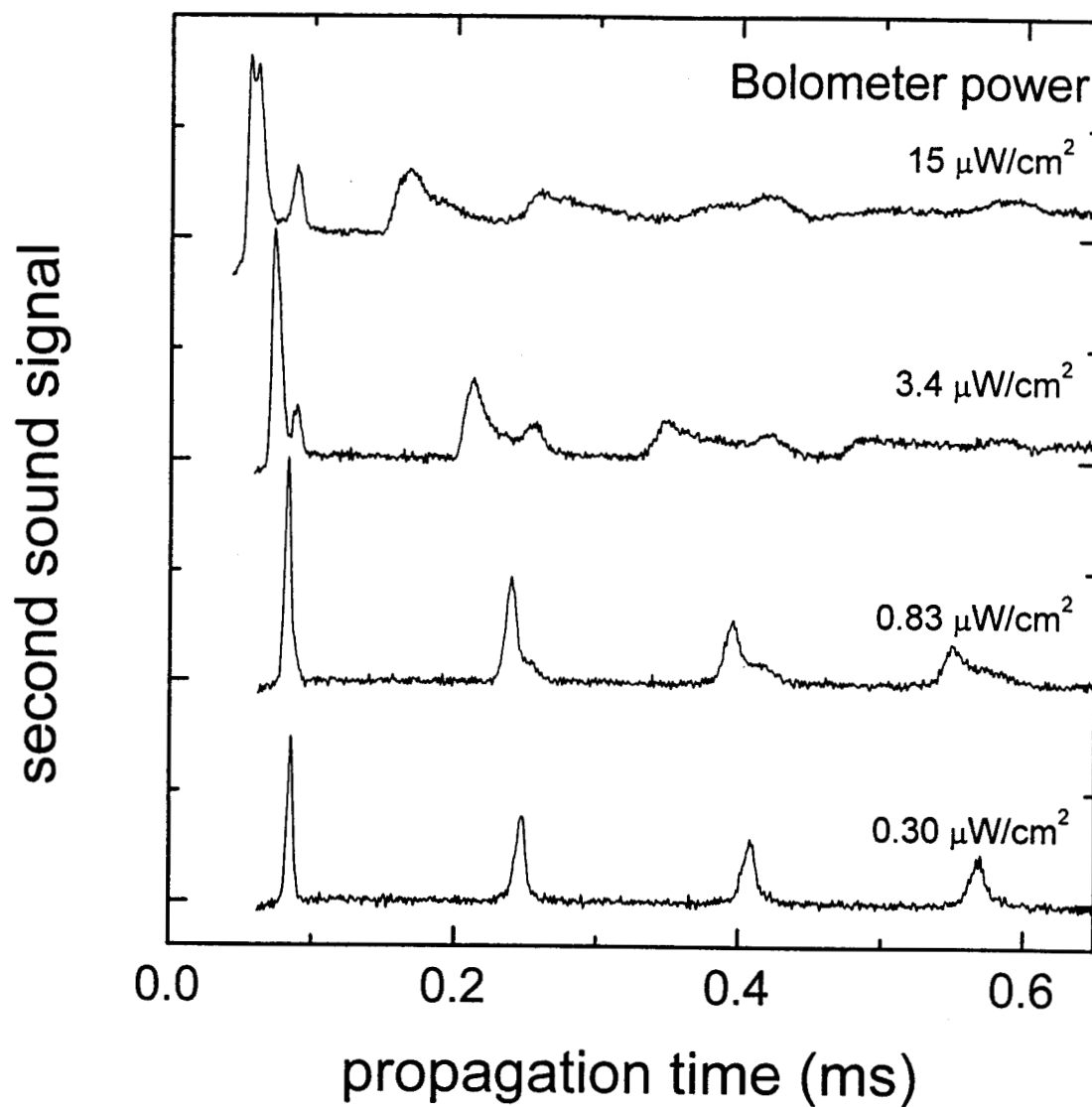
- Even at moderate distances to tricritical point
  - Second sound is very non-linear
    - Formation of shock tails
    - Large heat pulses
      - Saturation of second sound signal
        - » Previously seen in bulk helium-4, very close to  $T_\lambda$
  - Signals sensitive to bolometer power dissipation
    - Heat flush effect decreases  $^3\text{He}$  around bolometer
      - Speed of second sound increases
      - Large enough bolometer powers
        - » Signal splits
        - » One path through  $^3\text{He}$  depleted region
        - » Other path through unaffected regions

## Non-linear Saturation Effects

- Pure  $^4\text{He}$ 
  - $T_\lambda - T = 10\mu\text{K}$
  - heat pulse: 0.28ms
  - Heat flux from: 0.058 to 7.77 mW/cm<sup>2</sup>
- $^3\text{He}$ - $^4\text{He}$  Mixture ( $X_3=0.66$ )
  - $T_\lambda - T = 2.5\text{mK}$
  - heat pulse: 10, 15, & 20  $\mu\text{s}$
  - Heat flux: 64 mW/cm<sup>2</sup>

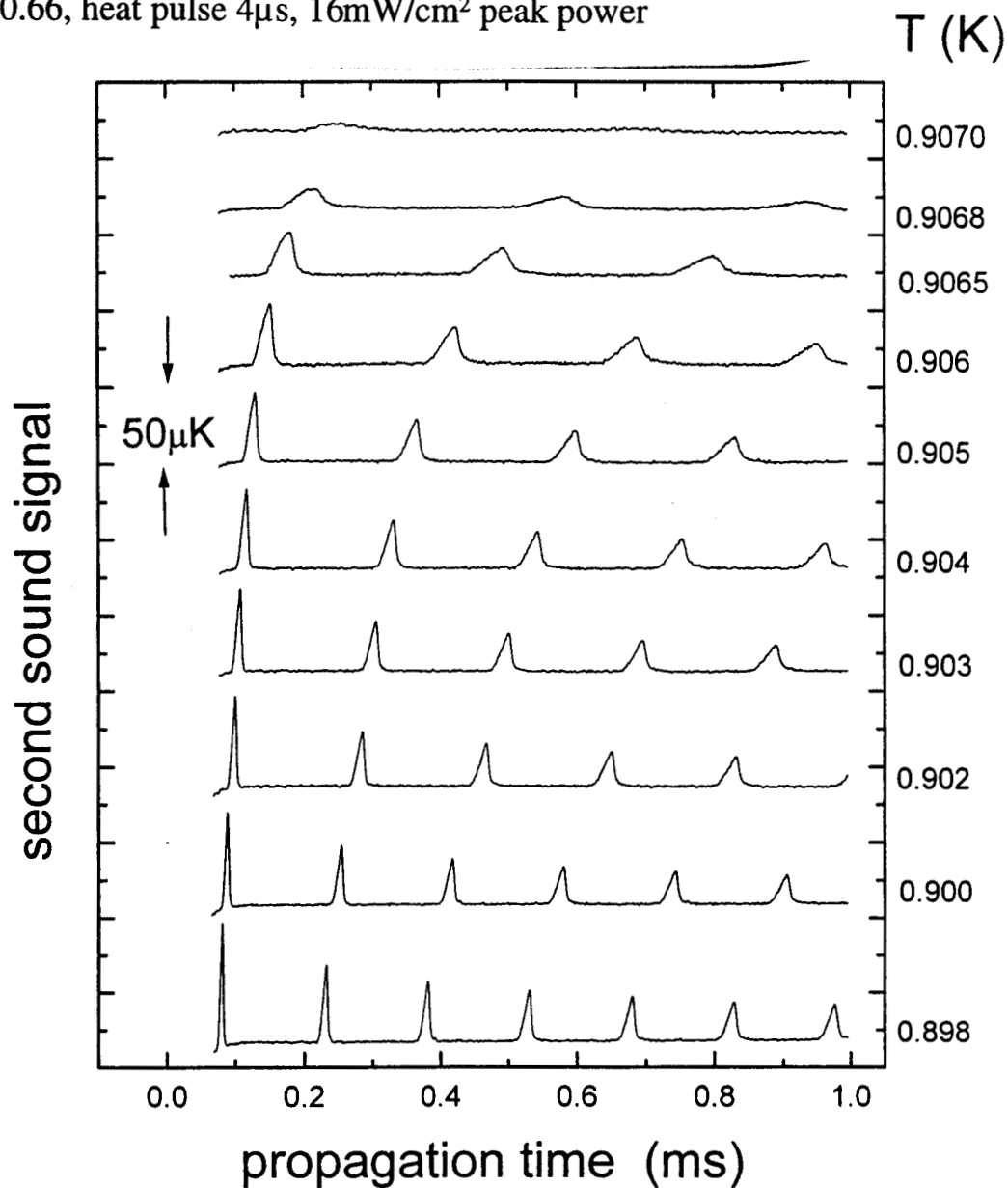


# Bolometer Power Effect



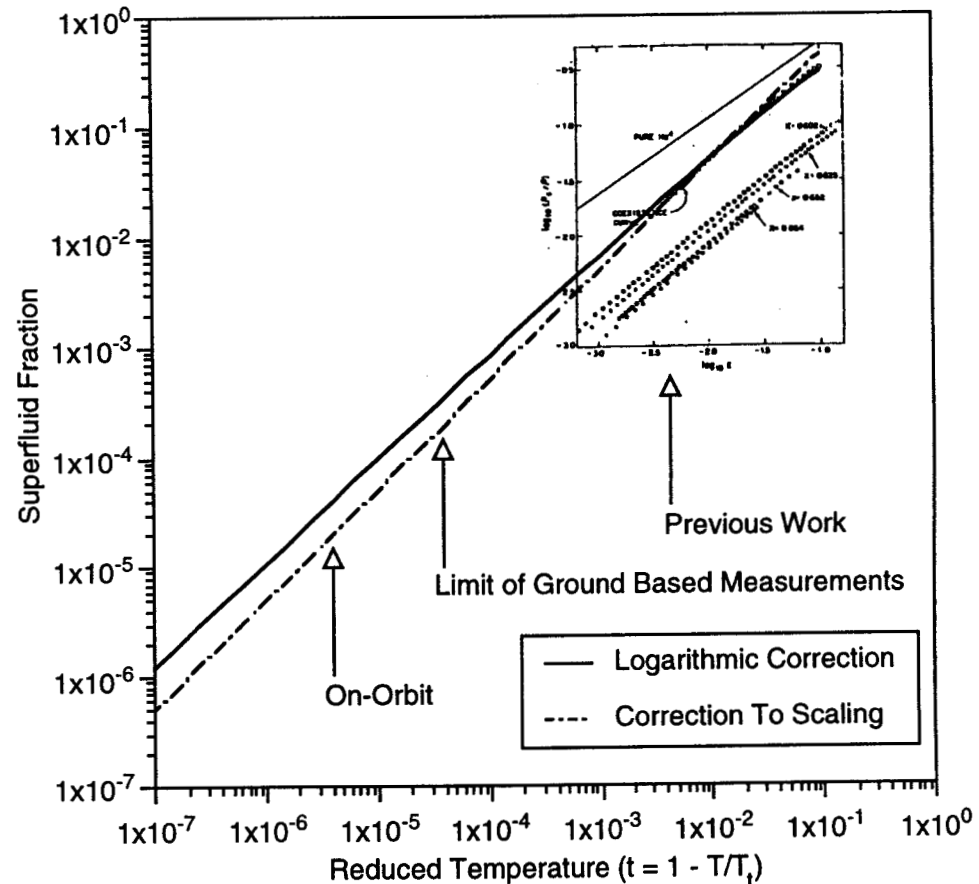
# Second Sound Approaching the Tricritical Point

–  $X_3 = 0.66$ , heat pulse  $4\mu\text{s}$ ,  $16\text{mW}/\text{cm}^2$  peak power



# Summary: Superfluid Density

- Ground based measurements will improve existing data by over one decade in reduced temperature
- Flight measurements will extend data another decade
- Will be able to distinguish logarithmic corrections from corrections to scaling



## Conclusions and Plans

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- Tricritical point is a rich area of study
- Tricritical behavior provides rigorous test of exact theoretical predictions of RG
- Modern technology can be applied to reach the fundamental measurement limits
- Refine the data reduction and analysis
  - Include the non-linear effects
- Finish the JPL sub-Kelvin facility
  - Technology development
  - Second science probe
- Refine the flight parameters

